Many computer applications involve sorting the items in a list into some specified order.

For example, we have seen that a list may be searched more efficiently if it is sorted.

To sort a group of items, the following relationships must be clearly defined over the items to be sorted:

\[
\begin{align*}
a & < b \\
a & > b \\
a & = b
\end{align*}
\]

Ascending order: smallest ... largest

Descending order: largest ... smallest

When designing or choosing an algorithm for sorting, one goal is to minimize the amount of work necessary to sort the list of items.

Generally the amount of work is measured by the number of comparisons of list elements and/or the number of swaps of list elements that are performed.
Bubble Sort Algorithm

One of the simplest sorting algorithms proceeds by walking down the list, comparing adjacent elements, and swapping them if they are in the wrong order. The process is continued until the list is sorted.

More formally:

1. Initialize the size of the list to be sorted to be the actual size of the list.

2. Loop through the list until no element needs to be exchanged with another to reach its correct position.
   
   2.1 Loop (i) from 0 to size of the list to be sorted - 2.
   
      2.1.1 Compare the \( i \)th and \((i + 1)\)st elements in the unsorted list.
      2.1.2 Swap the \( i \)th and \((i + 1)\)st elements if not in order (ascending or descending as desired).
   
   2.2 Decrease the size of the list to be sorted by 1.

Each pass "bubbles" the largest element in the unsorted part of the list to its correct location.

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<tr>
<th>13</th>
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A
Here is an ascending-order implementation of the bubblesort algorithm for integer arrays:

```c
void BubbleSort(int List[], int Size) {
    int tempInt; // temp variable for swapping list elems
    for (int Stop = Size - 1; Stop > 0; Stop--) {
        for (int Check = 0; Check < Stop; Check++) { // make a pass
            if (List[Check] > List[Check + 1]) { // compare elems
                tempInt = List[Check]; // swap if in the
                List[Check] = List[Check + 1]; // wrong order
                List[Check + 1] = tempInt;
            }
        }
    }
}
```

Bubblesort compares and swaps adjacent elements; simple but not very efficient.

Efficiency note: the outer loop could be modified to exit if the list is already sorted.
Trace the given implementation on the array below. Try to keep track of how many comparisons and swaps are performed.

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Pass 9
Selection Sort Algorithm

Another simple sorting algorithm proceeds by walking down the list, and finding the smallest (or largest) element, and then swapping it to the beginning of the unsorted part of the list. The process is continued until the list is sorted.

More formally:

1. Loop (i) from 0 to the (number of elements to be sorted - 2)
   1.1 Assume the smallest remaining item is at the i^th position, call this location smallest.
   1.2 Loop (j) through the remainder of the list to be sorted (i+1 .. size-1).
      1.2.1 Compare the j^th & smallest elements in the unsorted list.
      1.2.2 If the j^th element is < the smallest element then
          reset the location of the smallest to the j^th location.
   1.3 Move the smallest element to the head of the unsorted list,
       (i.e. swap the ith and smallest elements).

After sorting all but 1 element the remaining element must be in its correct position.
Here is an ascending-order implementation of the selection sort algorithm for integer arrays:

```c++
void SelectionSort(int List[], int Size) {
    int Begin, SmallSoFar, Check;
    void Swap(int& Elem1, int& Elem2); // see previous slide
    for (Begin = 0; Begin < Size - 1; Begin++) {
        SmallSoFar = Begin; // set head of tail
        for (Check = Begin + 1; Check < Size; Check++) { // scan current tail
            if (List[Check] < List[SmallSoFar])
                SmallSoFar = Check;
        }
        Swap(List[Begin], List[SmallSoFar]); // put smallest elem at front
    } // of current tail
}

void Swap(int& Elem1, int& Elem2) {
    int tempInt;
    tempInt = Elem1;
    Elem1 = Elem2;
    Elem2 = tempInt;
}
```
Trace the given implementation on the array below. Try to keep track of how many comparisons and swaps are performed.

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</table>
Here is an ascending-order implementation of the bubble sort algorithm for integer arrays:

```c++
void sortByOrigin(Trip dB[], int numTrips) {
    Trip tempTrip;    // temp variable for swapping list elems
    for (int Stop = numTrips - 1; Stop > 0; Stop--) {
        for (int Check = 0; Check < Stop; Check++) { // make a pass
            // compare Origin fields of array elements
            if (dB[Check].Origin > dB[Check + 1].Origin) {
                tempTrip = dB[Check];     // swap if in the
                dB[Check] = dB[Check + 1]; //   wrong order
                dB[Check + 1] = tempTrip;
            }
        }
    }
}
```