The only teaching that a professor can give, in my opinion, is that of thinking in front of his students.

Henri Lebesgue

Men occasionally stumble over the truth, but most of them pick themselves up and hurry off as if nothing ever happened.

Winston Churchill
Learning a Skill

In general, to learn a skill (golf, driving car):
- The skill is demonstrated to student.
- The student is directed and guided while practicing.

What about analytical reasoning skills?
- It goes on inside the head – hard to demonstrate.
- It is hard to direct and guide the student.
The most effective way to expose the process is to verbalize our thinking process

This is hard work! It is not our normal mode of behavior.
Need to be careful to explain every step.
Need to address alternative valid analyses.
Also need to create and discuss blind alleys.

We can demonstrate analytical reasoning by watching problem solvers solve problems while thinking aloud.

You will practice problem solving by thinking aloud to a partner.
We will use the technique of Whimbey & Lochhead.

The partners have distinct roles:

One partner should read and think aloud.

On some assignments, the solver will be the scribe as well.

The other partner is the listener.

Continually checks the accuracy of the solver's work.

Demands constant vocalization from the solver.

Thinking is a skill… but it is largely invisible.

So we need to do everything possible to make it visible during this process.

Adaptation to small groups:

May have single solver and multiple listeners, or

multiple solvers and multiple listeners, and/or

assign role of scribe to a different group member.
Problem 1

If the circle below is taller than the square and the cross is shorter than the square, put a K in the circle. However, if this is not the case, put a T in the second tallest figure.

K

T
Characteristics of Good Problem Solvers

Maintain a positive attitude.

Hold the belief that academic reasoning problems can be solved through persistence, as opposed to believing “either you know it or you don’t”.

Engage fully when dealing with a confusing problem.

Maintain a concern for accuracy.

Actively work to check your understanding

Decompose the problem into simpler parts.

Avoid guessing.

And don’t jump to conclusions.

Be active in problem solving.

Do more things as part of the process.
Problem 2

If the word *sentence* contains less than 9 letters and more than 3 vowels, circle the first vowel. Otherwise circle the consonant that is farthest to the right in the word.

*sentence*
Role of the Listener

This is a crucial role, and takes hard work. It is not a passive role!

1. Continually check accuracy.
   - Catch errors
   - Must work along/understand every step
   - Don’t let solver get ahead of him/herself
   - Point out errors, do not correct

2. Demand constant vocalization.
   - Solver must spell out EVERY step
   - On assignments, solver must make notes on EVERY step

3. Use Socratic questioning (Fogler/LeBlanc, p. 89—92).
Bill, Judy, and Sally have the occupations of teacher, plumber, and teamster but not necessarily in that order. Bill is shorter than Judy but taller than Sally. The plumber is the tallest and teamster is the shortest. What is Judy’s occupation?
If the second letter in the word west comes after the fourth letter in the alphabet, circle the letter A below. If it does not, circle the B.

A   B
Problem 5

Give a rough estimate of the number of telephones on the Virginia Tech campus.
Problem 6

You drive a car at a constant speed of 40 mph from A to B, and on arrival at B, you return immediately to A but at a higher constant speed of 60 mph.

What was your average speed for the whole trip?
“Eighty percent of success is showing up.”
   Woody Allen

“Success is 1% inspiration and 99% perspiration.”
   Thomas Edison

To successfully solve any problem, the most important step is to get actively involved.
   The Principle of Intimate Engagement: You must commit to the problem
   “Roll up your sleeves”
   “Get your hands dirty.”