CS 4604: Introduction to Database Management Systems

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Lecture #8: Indexes and Hashing
Announcements

- Check the office hours schedule on Piazza.
  - Several extra ones
  - My Wed office hour this week Feb 24 is canceled

- On Wed Feb 24:
  - Shamimul and Sorour will give the lecture on (maybe) some hashing and Sorting.
DBMS Layers:

- Query Optimization and Execution
- Relational Operators
- Files and Access Methods
- Buffer Management
- Disk Space Management

TODAY → DB
Leverage OS for disk/file management?

- Layers of abstraction are good ... but:
Leverage OS for disk/file management?

- Layers of abstraction are good ... but:
  - Unfortunately, OS often gets in the way of DBMS
Leverage OS for disk/file management?

- DBMS wants/needs to do things “its own way”
  - Specialized prefetching
  - Control over buffer replacement policy
    - LRU not always best (sometimes worst!!)
  - Control over thread/process scheduling
    - “Convoy problem”
      - Arises when OS scheduling conflicts with DBMS locking
  - Control over flushing data to disk
    - WAL protocol requires flushing log entries to disk
DBMS stores information on disks.

– but: disks are (relatively) VERY slow!

Major implications for DBMS design!
Major implications for DBMS design:

- **READ**: disk -> main memory (RAM).
- **WRITE**: reverse

- Both are high-cost operations, relative to in-memory operations, so must be planned carefully!
Why Not Store It All in Main Memory?
Why Not Store It All in Main Memory?

- **Costs too much.**
  - disk: ~$1/Gb; memory: ~$100/Gb
  - High-end Databases today in the 10-100 TB range.
  - Approx 60% of the cost of a production system is in the disks.

- **Main memory is volatile.**

- **Note:** some specialized systems do store entire database in main memory.
The Storage Hierarchy

Smaller, Faster

Bigger, Slower
The Storage Hierarchy

- Main memory (RAM) for currently used data.
- Disk for the main database (secondary storage).
- Tapes for archiving older versions of the data (tertiary storage).

![Diagram showing the storage hierarchy with levels from smaller, faster to bigger, slower](image-url)

Registers

L1 Cache

Main Memory

Magnetic Disk

Magnetic Tape

Smaller, Faster

Bigger, Slower
Jim Gray’s Storage Latency Analogy: How Far Away is the Data?

- **Tape**: $10^9$ (Andromeda), 2,000 Years
- **Disk**: $10^6$, 2 Years
- **Memory**: 100, 1.5 hr
- **On Board Cache**: 10, 10 min
- **On Chip Cache**: 2, 10 min
- **Registers**: 1, 1 min
- **This Reading**: Pluto, 2,000 Years
- **This Room**: Andromeda, 2,000 Years
- **This Building**: Boston, 1.5 hr
- **My Head**: 1 min
Disks

- Secondary storage device of choice.
- Main advantage over tapes: *random access* vs. *sequential*.
- Data is stored and retrieved in units called *disk blocks* or *pages*.
- Unlike RAM, time to retrieve a disk page varies depending upon location on disk.
  - relative placement of pages on disk is important!
Anatomy of a Disk

- Sector
- Track
- Cylinder
- Platter
- Block size = multiple of sector size (which is fixed)
Accessing a Disk Page

- Time to access (read/write) a disk block:
  - .
  - .
  - .
Accessing a Disk Page

- Time to access (read/write) a disk block:
  - *seek time*: moving arms to position disk head on track
  - *rotational delay*: waiting for block to rotate under head
  - *transfer time*: actually moving data to/from disk surface
Accessing a Disk Page

- Relative times?
  - seek time:
  - rotational delay:
  - transfer time:
Accessing a Disk Page

- Relative times?
  - *seek time*: about 1 to 20msec
  - *rotational delay*: 0 to 10msec
  - *transfer time*: < 1msec per 4KB page
Seek time & rotational delay dominate

- Key to lower I/O cost: reduce seek/rotation delays!
- Also note: For shared disks, much time spent waiting in queue for access to arm/controller
Arranging Pages on Disk

- "Next" block concept:
  - blocks on same track, followed by
  - blocks on same cylinder, followed by
  - blocks on adjacent cylinder

- Accessing ‘next’ block is cheap

- A useful optimization: pre-fetching
  - See textbook page 323
Rules of thumb...

1. Memory access much faster than disk I/O (~ 1000x)
   - “Sequential” I/O faster than “random” I/O (~ 10x)
Conclusions---Storing

- Memory hierarchy
- Disks: (>1000x slower) - thus
  - pack info in blocks
  - try to fetch nearby blocks (sequentially)
TREE INDEXES
Declaring Indexes

- No standard!
- Typical syntax:

CREATE INDEX StudentsInd ON Students(ID);

CREATE INDEX CoursesInd ON Courses(Number, DeptName);
Types of Indexes

- **Primary**: index on a key
  - Used to enforce constraints

- **Secondary**: index on non-key attribute

- **Clustering**: order of the rows in the data pages correspond to the order of the rows in the index
  - Only one clustered index can exist in a given table
  - Useful for range predicates

- **Non-clustering**: physical order not the same as index order
Using Indexes (1): Equality Searches

- Given a value \( v \), the index takes us to only those tuples that have \( v \) in the attribute(s) of the index.

- E.g. (use CourseInd index)

```
SELECT Enrollment FROM Courses
WHERE Number = "4604" and DeptName = "CS"
```
Using Indexes (1): Equality Searches

- Given a value \( v \), the index takes us to only those tuples that have \( v \) in the attribute(s) of the index.

- Can use Hashes, but see next
Using Indexes (2): Range Searches

- ``Find all students with gpa > 3.0’ ’
- may be slow, even on sorted file
- Hashes not a good idea!
- What to do?
Range Searches

- ``Find all students with gpa > 3.0' '
- may be slow, even on sorted file
- Solution: Create an `index' file.

```
Find all students with gpa > 3.0
may be slow, even on sorted file
Solution: Create an `index' file.
```
Range Searches

- More details:
- if index file is small, do binary search there
- Otherwise??
B-trees

- the most successful family of index schemes (B-trees, B+-trees, B*-trees)
- Can be used for primary/secondary, clustering/non-clustering index.
- balanced “n-way” search trees
B-trees

- Eg., B-tree of order d=1:
B - tree properties:

- each node, in a B-tree of order d:
  - Key order
  - at most n=2d keys
  - at least d keys (except root, which may have just 1 key)
  - all leaves at the same level
  - if number of pointers is k, then node has exactly k-1 keys
  - (leaves are empty)
Properties

- “block aware” nodes: each node is a disk page
- $O(\log(N))$ for everything! (ins/del/search)
- typically, if $d = 50 - 100$, then 2 - 3 levels
- utilization $\geq 50\%$, guaranteed; on average 69\%
Queries

- Algo for exact match query? (eg., ssn=8?)
JAVA animation

- http://slady.net/java/bt/
Queries

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Queries

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Queries

- what about range queries? (eg., 5<salary<8)
- Proximity/ nearest neighbor searches? (eg., salary ~ 8 )
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Variations

- How could we do even better than the B-trees above?
B+ trees - Motivation

- B-tree – print keys in sorted order:
B+ trees - Motivation

- B-tree needs back-tracking – how to avoid it?
B+ trees - Motivation

- Stronger reason: for clustering index, data records are scattered:
Solution: B+ - trees

- facilitate sequential ops
- They string all leaf nodes together
- AND
- replicate keys from non-leaf nodes, to make sure every key appears at the leaf level
- (vital, for clustering index!)
B+ trees
B+ trees

Index Pages

Data Pages
B+ trees

- More details: next (and textbook)
- In short: on split
  - at leaf level: COPY middle key upstairs
  - at non-leaf level: push middle key upstairs (as in plain B-tree)
Example B+ Tree

- Search begins at root, and key comparisons direct it to a leaf
- Search for 5*, 15*, all data entries >= 24* ...

Based on the search for 15*, we know it is not in the tree!
Inserting a Data Entry into a B+ Tree

- Find correct leaf L.
- Put data entry onto L.
  - If L has enough space, done!
  - Else, must split L (into L and a new node L2)
    - Redistribute entries evenly, copy up middle key.
- parent node may overflow
  - but then: push up middle key. Splits “grow” tree; root split increases height.
Example B+ Tree – Inserting 30*
Example B+ Tree – Inserting 30*

Root

2* 3* 5* 7*

14* 16*

19* 20* 22* 23*

24* 27* 29* 30*
Example B+ Tree - Inserting 8*
Example B+ Tree - Inserting 8*

No Space
Example B+ Tree - Inserting 8*

So Split!
Example B+ Tree - Inserting 8*

So Split!

And then push middle UP
Example B+ Tree - Inserting 8*

Final State
Example B+ Tree - Inserting 21*
Example B+ Tree - Inserting 21*

Root

Root is Full, so split recursively
Example B+ Tree: Recursive split

- Notice that root was also split, increasing height.
Example: Data vs. Index Page Split

- leaf: ‘copy’
- non-leaf: ‘push’

why not ‘copy’ @ non-leaves?
Same Inserting 21*: The Deferred Split

Note this has free space. So...
Inserting 21*: The Deferred Split

LEND keys to sibling, through PARENT!
Inserting 21*: The Deferred Split

Shorter, more packed, faster tree
Insertion examples for you to try

Insert the following data entries (in order): 28*, 6*, 25*
Answer...

After inserting 28*, 6*

After inserting 25*
After inserting 25*
Deleting a Data Entry from a B+ Tree

- Start at root, find leaf L where entry belongs.
- Remove the entry.
  - If L is at least half-full, done!
  - If L underflows
    - Try to re-distribute, borrowing from sibling (adjacent node with same parent as L).
    - If re-distribution fails, merge L and sibling.
      - update parent
      - and possibly merge, recursively
Deletion from B+Tree

Root

2* 3* 5* 7* 8* 14* 16* 19* 20* 21* 22* 23* 24* 27* 29*
Example: Delete 19* & 20*

Deleting 19* is easy:

• Deleting 20* -> re-distribution (notice: 27 copied up)
... And Then Deleting 24*

Must merge leaves: OPPOSITE of insert
... And Then Deleting 24*

Praka: • Must merge leaves: OPPOSITE of insert
... Merge Non-Leaf Nodes, Shrink Tree

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Example of Non-leaf Re-distribution

- Tree is shown below during deletion of 24*.
- Now, we can re-distribute keys
need only re-distribute ‘20’; did ‘17’, too
why would we want to re-distribute more keys?
Main observations for deletion

- If a key value appears twice (leaf + nonleaf), the above algorithms delete it from the leaf, only
- why not non-leaf, too?
Main observations for deletion

- If a key value appears twice (leaf + nonleaf), the above algorithms delete it from the leaf, only
- why not non-leaf, too?
- ‘lazy deletions’ - in fact, some vendors just mark entries as deleted (~ underflow), – and reorganize/compact later
Recap: main ideas

- on overflow, split (and ‘push’, or ‘copy’)  
  – or consider deferred split

- on underflow, borrow keys; or merge  
  – or let it underflow...
B+ Trees in Practice

- Typical order: 100. Typical fill-factor: 67%.
  - average fanout = 2*100*0.67 = 134

- Typical capacities:
  - Height 4: 1334 = 312,900,721 entries
  - Height 3: 1333 = 2,406,104 entries
B+ Trees in Practice

- Can often keep top levels in buffer pool:
  - Level 1 = 1 page = 8 KB
  - Level 2 = 134 pages = 1 MB
  - Level 3 = 17,956 pages = 140 MB
Bulk Loading of a B+ Tree

- In an empty tree, insert many keys
- Why not one-at-a-time?
  - Too slow!
Bulk Loading of a B+ Tree

- Initialization: Sort all data entries
- scan list; whenever enough for a page, pack
- <repeat for upper level>
Bulk Loading of a B+ Tree

Data entry pages not yet in B+ tree

Data entry pages not yet in B+ tree
A Note on `Order’

- Order (d) concept replaced by physical space criterion in practice (‘at least half-full’).
- Many real systems are even sloppier than this: they allow underflow, and only reclaim space when a page is completely empty.
- (what are the benefits of such ‘slopiness’?)
Conclusions

- B+tree is the prevailing indexing method
- Excellent, $O(\log N)$ worst-case performance for ins/del/search; (~3-4 disk accesses in practice)
- guaranteed 50% space utilization; avg 69%
Conclusions

- Can be used for any type of index: primary/secondary, sparse (clustering), or dense (non-clustering)
- Several fine-extensions on the basic algorithm
  - deferred split;
  - bulk-loading
HASHING
(Static) Hashing

- Problem: “find EMP record with ssn=123”
- What if disk space was free, and time was at premium?
Hashing

- A: Brilliant idea: key-to-address transformation:

123; Smith; Main str

#0 page
#123 page
#999,999,999
Since space is NOT free:
- use M, instead of 999,999,999 slots
- hash function: \( h(key) = \text{slot-id} \)
Hashing

- Typically: each hash bucket is a page, holding many records:

123; Smith; Main str

#h(123)

#0 page

M
Hashing

- Notice: could have clustering, or non-clustering versions:

#0 page

#h(123)

M

123; Smith; Main str.
Hashing

- Notice: could have clustering, or non-clustering versions:

```
#0 page

#h(123)

123

M

EMP file

234; Johnson; Forbes ave
123; Smith; Main str.
345; Tompson; Fifth ave
```
Design decisions

- 1) formula $h()$ for hashing function
- 2) size of hash table $M$
- 3) collision resolution method
Problem with static hashing

- problem: overflow?
- problem: underflow? (underutilization)
Solution: Dynamic/extendible hashing

- idea: shrink / expand hash table on demand..
- ..dynamic hashing
- Details: how to grow gracefully, on overflow?
- Many solutions - One of them: ‘extendible hashing’ [Fagin et al]
Extendible hashing

123; Smith; Main str. → #h(123)

#0 page → M

FULL
Extendible hashing

solution:

split the bucket in two

123; Smith; Main str.
in detail:

- keep a directory, with ptrs to hash-buckets
- Q: how to divide contents of bucket in two?
- A: hash each key into a very long bit string; keep only as many bits as needed

Eventually:
Extendible hashing

directory

00...
01...
10...
11...

0001...
0111...
10101...
10011...
1101...
0111...
0001...
101001...

10110...
10110...

Extendible hashing

Directory

00...
01...
10...
11...

0001...
0111...

10101...
10011...
10110...

1101...

101001...
Extendible hashing

directory

split on 3-rd bit
Extendible hashing

(directory

00...
01...
10...
11...

0001...
0111...

10011...

101001...
10101...
10110...

1101...

10101...
101001...
10110...
Extendible hashing

directory (doubled)

000...
001...
010...
011...
100...
101...
110...
111...

new page / bucket

0001...
0111...
10011...
10011...
101001...
10101...
10110...

10011...
101001...
10110...

1101...

Extendible hashing

BEFORE

AFTER

00...
01...
10...
11...

0001...
0111...
10101...
10011...
1101...
10011...

0000...
0010...
0100...
0110...
1000...
1010...
1100...
1110...

101001...
10101...
101001...
10110...
1101...
1101...

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Extendible hashing

- Summary: directory doubles on demand or halves, on shrinking files
- needs ‘local’ and ‘global’ depth