

CS 4604: Introduction to Database Management Systems

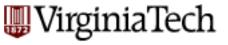
B. Aditya Prakash

Lecture #2: The Relational Model and Relational Algebra

Course Outline

- Weeks 1–4: Query/ Manipulation Languages and Data Modeling
 - Relational Algebra
 - Data definition
 - Programming with SQL
 - Entity-Relationship (E/R) approach
 - Specifying Constraints
 - Good E/R design
- Weeks 5–8: Indexes, Processing and Optimization
 - Storing
 - Hashing/Sorting
 - Query Optimization
 - NoSQL and Hadoop

- Week 9-10: Relational Design
 - Functional Dependencies
 - Normalization to avoid redundancy
- Week 11-12: Concurrency Control
 - Transactions
 - Logging and Recovery
- Week 13–14: Students' choice
 - Practice Problems
 - XML
 - Data mining and warehousing



Data Model

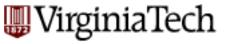
- A Data Model is a notation for describing data or information.
 - Structure of data (e.g. arrays, structs)
 - Conceptual model: In databases, structures are at a higher level.
 - Operations on data (Modifications and Queries)
 - Limited Operations: Ease of programmers and efficiency of database.
 - Constraints on data (what the data can be)
- Examples of data models
 - The Relational Model
 - The Semistructured-Data Model
 - XML and related standards
 - Object-Relational Model



The Relational Model

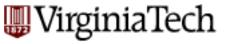
Student	Course	Grade
Hermione Grainger	Potions	А
Draco Malfoy	Potions	В
Harry Potter	Potions	А
Ron Weasley	Potions	С

- Structure: Table (like an array of structs)
- Operations: Relational alebgra (selection, projection, conditions, etc)
- Constraints: E.g., grades can be only {A, B, C, F}



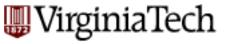
The Semi-structured model

- Structure: Trees or graphs, tags define role played by different pieces of data.
- Operations: Follow paths in the implied tree from one element to another.
- Constraints: E.g., can express limitations on data types



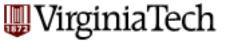
Comparing the two models

- Flexibility: XML can represent graphs
- Ease of use: SQL enables programmer to express wishes at high level.



The Relational Model

- Simple: Built around a single concept for modeling data: the relation or table.
 - A relational database is a collection of relations.
 - Each relation is a table with rows and columns.
- Supports high-level programming language (SQL).
 - Limited but very useful set of operations
- Has an elegant mathematical design theory.
- Most current DBMS are relational (Oracle, IBM DB2, MS SQL)



Relations

- A relation is a two-dimensional table:
 - Relation == table.
 - Attribute == column name.
 - Tuple == row (not the header row).
- Database == collection of relations.
- A relation has two parts:
 - Schema defines column heads of the table (attributes).
 - Instance contains the data rows (tuples, rows, or records) of the table.

Student	Course	Grade
Hermione Grainger	Potions	Α
Draco Malfoy	Potions	В
Harry Potter	Potions	А
Ron Weasley	Potions	С

Prakash 2016



Schema

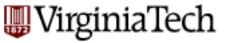
CoursesTaken:

Student	Course	Grade
Hermione Grainger	Potions	А
Draco Malfoy	Potions	В
Harry Potter	Potions	А
Ron Weasley	Potions	С

 The schema of a relation is the name of the relation followed by a parenthesized list of attributes.

CoursesTaken (Student, Course, Grade)

- A design in a relational model consists of a set of schemas.
- Such a set of schemas is called a relational database schema.



Relations: Equivalent Representations

CoursesTaken:

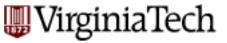
Student	Course	Grade
Hermione Grainger	Potions	А
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Harry Potter	Potions	Α
Ron Weasley	Potions	С

CoursesTaken(Student, Course, Grade)

- Relation is a <u>set</u> of tuples and not a list of tuples.
 - Order in which we present the tuples does not matter.
 - Very important!
- The attributes in a schema are also a <u>set</u> (not a list).
 - Schema is the same irrespective of order of attributes.

CoursesTaken (Student, Grade, Course)

- We specify a "standard" order when we introduce a schema.
- How many equivalent representations are there for a relation with m attributes and n tuples?



Degree and Cardinality

CoursesTaken:

Student	Course	Grade
Hermione Grainger	Potions	А
Draco Malfoy	Potions	В
Harry Potter	Potions	А
Ron Weasley	Potions	С

- Degree/Arity is the number of fields/attributes in schema (=3 in the table above)
- Cardinality is the number of tuples in relation (=4 in the table above)



Keys of Relations

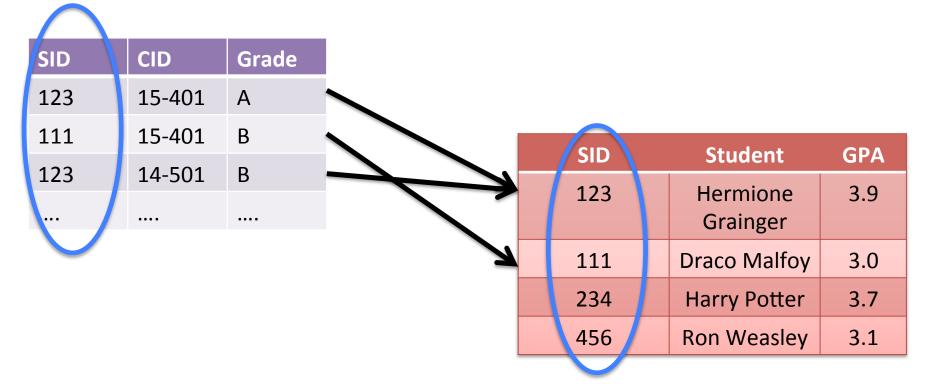
- Keys are one form of integrity constraints (IC)
 - No pair of tuples should have identical keys
- What is the key for CoursesTaken?
 - Student if only one course in the relation
 - Pair (Student, Course) if multiple courses
 - What if student takes same course many times?

Student	Course	Grade
Hermione Grainger	Potions	А
Draco Malfoy	Potions	В
Harry Potter	Potions	А
Ron Weasley	Potions	С



Keys of Relations

 Keys help associate tuples in different relations





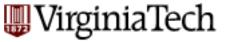
Example

Create a database for managing class enrollments in a single semester. You should keep track of all students (their names, Ids, and addresses) and professors (name, Id, department). Do not record the address of professors but keep track of their ages. Maintain records of courses also. Like what classroom is assigned to a course, what is the current enrollment, and which department offers it. At most one professor teaches each course. Each student evaluates the professor teaching the course. Note that all course offerings in the semester are unique, i.e. course names and numbers do not overlap. A course can have ≥ 0 pre-requisites, excluding itself. A student enrolled in a course must have enrolled in all its pre-requisites. Each student receives a grade in each course. The departments are also unique, and can have at most one chairperson (or dept. head). A chairperson is not allowed to head two or more departments.



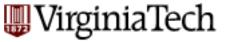
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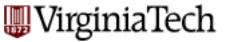
Relational Design for the Example

- Students (PID: string, Name: string, Address: string)
- Professors (PID: string, Name: string, Office: string, Age: integer, DepartmentName: string)
- Courses (Number: integer, DeptName: string, CourseName: string, Classroom: string, Enrollment: integer)
- Teach (ProfessorPID: string, Number: integer, DeptName: string)
- Take (StudentPID: *string*, Number: *integer*, DeptName: *string*, Grade: *string*, ProfessorEvaluation: integer)
- Departments (Name: string, ChairmanPID: string)
- PreReq (Number: integer, DeptName: string, PreReqNumber: integer, PreReqDeptName: string)



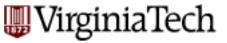
Relational Design Example: Keys?

- Students (PID: string, Name: string, Address: string)
- Professors (PID: string, Name: string, Office: string, Age: integer, DepartmentName: string)
- Courses (Number: integer, DeptName: string, CourseName: string, Classroom: string, Enrollment: integer)
- Teach (ProfessorPID: string, Number: integer, DeptName: string)
- Take (StudentPID: *string*, Number: *integer*, DeptName: *string*, Grade: *string*, ProfessorEvaluation: integer)
- Departments (Name: string, ChairmanPID: string)
- PreReq (Number: integer, DeptName: string, PreReqNumber: integer, PreReqDeptName: string)



Relational Design: Keys?

- Students (<u>PID</u>: <u>string</u>, Name: <u>string</u>, Address: <u>string</u>)
- Professors (<u>PID</u>: <u>string</u>, Name: <u>string</u>, Office: <u>string</u>, Age: <u>integer</u>,
 DepartmentName: <u>string</u>)
- Courses (<u>Number: integer</u>, DeptName: *string*, CourseName: *string*, Classroom: *string*, Enrollment: *integer*)
- Teach (ProfessorPID: string, Number: integer, DeptName: string)
- Take (<u>StudentPID</u>: <u>string</u>, <u>Number</u>: <u>integer</u>, <u>DeptName</u>: <u>string</u>, Grade: <u>string</u>,
 ProfessorEvaluation: integer)
- Departments (<u>Name</u>: <u>string</u>, ChairmanPID: <u>string</u>)
- PreReq (<u>Number</u>: <u>integer</u>, <u>DeptName</u>: <u>string</u>, <u>PreReqNumber</u>: <u>integer</u>,
 <u>PreReqDeptName</u>: <u>string</u>)



Issues to Consider in the Design

- Can we merge Courses and Teach since each professor teaches at most one course?
- Do we need a separate relation to store evaluations?
- How can we handle pre-requisites that are "or"s, e.g., you can take CS 4604 if you have taken either CS 3114 or CS 2606?
- How do we generalize this schema to handle data over more than one semester?
- What modifications does the schema need if more than one professor can teach a course?

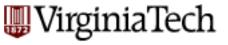


Formal query languages

- How do we collect information?
- Eg., find ssn's of people in 415
- (recall: everything is a set!)
- One solution: Rel. algebra, ie., set operators
- Q1: Which ones??
- Q2: what is a minimal set of operators?



- set union
- set difference '-'

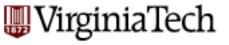


Example:

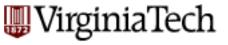
- Q: find all students (part or full time)
- A: PT-STUDENT union FT-STUDENT

FT-STUDENT		
<u>Ssn</u>	Name	
129	peters	main str
239	lee	5th ave

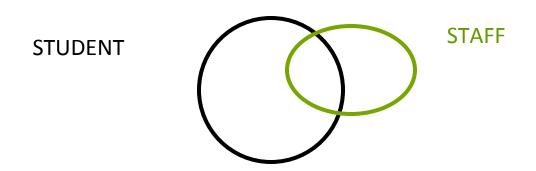
PT-STUDENT		
<u>Ssn</u>	Name	Address
123	smith	main str
234	jones	forbes ave

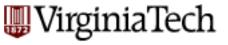


- two tables are 'union compatible' if they have the same attributes ('domains')
- Q: how about intersection

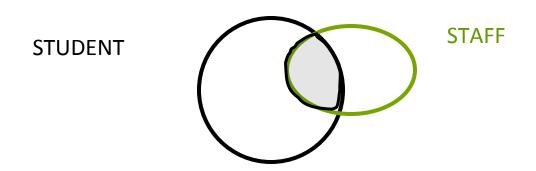


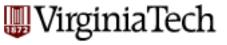
- A: redundant:
- STUDENT intersection STAFF =





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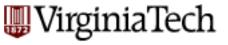




- A: redundant:
- STUDENT intersection STAFF = STUDENT - (STUDENT - STAFF)

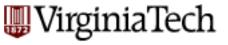
STUDENT

STAFF



- A: redundant:
- STUDENT intersection STAFF = STUDENT - (STUDENT - STAFF)

Double negation: We'll see it again, later...



- •

- set union
- set difference '-'



Other operators?

- eg, find all students on 'Main street'
- A: 'selection'

$$\sigma_{address='mainstr'}$$
 (STUDENT)

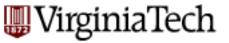
STUDENT		
Ssn	Name	Address
123	smith	main str
234	jones	forbes ave



Other operators?

- Notice: selection (and rest of operators)
 expect tables, and produce tables (-> can be cascaded!!)
- For selection, in general:

 $\sigma_{condition}$ (RELATION)

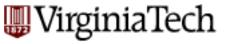


Selection - examples

Find all 'Smiths' on 'Main St.'

$$\sigma_{name='Smith' \land address='Main \ st.'}(STUDENT)$$

'condition' can be any boolean combination of '=', '>', '>=', '<>', ...



selection

 $\sigma_{\scriptscriptstyle condition}$

(R)

set union

RuS

set difference

R-S



- selection picks rows how about columns?
- A: 'projection' eg.:

$$\pi_{ssn}(STUDENT)$$

finds all the 'ssn' - removing duplicates

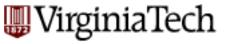
STUDENT		
<u>Ssn</u>	Name	Address
123	smith	main str
234	jones	forbes ave



Cascading: 'find ssn of students on 'main st.'

$$\pi_{ssn}(\sigma_{address='main\ st'}(STUDENT))$$

STUDENT		
<u>Ssn</u>	Name	Address
123	smith	main str
234	jones	forbes ave



$$\sigma_{condition}$$
 (R)

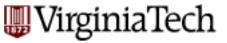
$$\pi_{_{att-list}}(R)$$

set union

 $R \cup S$

set difference

R-S



Are we done yet?

Q: Give a query we can **not** answer yet!



Relational operators

A: any query across **two** or more tables, eg., 'find names of students in 4604'

Q: what extra operator do we need??

STUDENT		
<u>Ssn</u>	Name	Address
123	smith	main str
234	jones	forbes ave

<u>SSN</u>	<u>c-id</u>	grade
123	4604	Α
234	5614	В



Relational operators

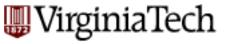
A: any query across **two** or more tables, eg., 'find names of students in 4604'

Q: what extra operator do we need??

A: surprisingly, cartesian product is enough!

STUDENT		
<u>Ssn</u>	Name	Address
123	smith	main str
234	jones	forbes ave

<u>SSN</u>	<u>c-id</u>	grade
123	4604	Α
234	5614	В



Cartesian product

- eg., dog-breeding: MALE x FEMALE
- gives all possible couples

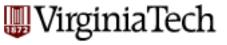
MALE		FEMALE
<u>name</u>	X	name
spike		lassie
spot		shiba

M.name	F.name
spike	lassie
spike	shiba
spot	lassie
spot	shiba



so what?

Eg., how do we find names of students taking 4604?



Cartesian product

• A: $\sigma_{STUDENT.ssn=TAKES.ssn}(STUDENT \ x \ TAKES)$

<u>Ssn</u>	Name	Address	ssn	cid	grade
123	smith	main str	123	4604	Α
	!	fouls a serve	400	4004	Λ
Z 34	jones	ioibes ave	123	4604	A
123	smith	main str	234	5614	R
	-				
234	jones	forbes ave	234	5614	В



Cartesian product

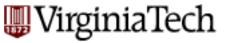
..
$$\sigma_{cid=4604}(\sigma_{STUDENT.ssn=TAKES.ssn}(STUDENT \ x \ TAKES))$$

<u>Ssn</u>	Name	Address	ssn	cid	grade
123	smith	main str	123	4604	Α
-224	jones	forhes ave	422	4604	_
		torbes ave	123		
∣ –123	-smith-	main str	234	5614	₽
234	iones	forbes ave	234	5614	В



```
\pi_{name}( \sigma_{cid=4604}(\sigma_{STUDENT.ssn=TAKES.ssn}(STUDENT~x~TAKES)) )
```

<u>Ssn</u>	Name	Address	ssn	cid	grade
12	23 smith	main str	123	4604	Α
	4 innes	forhes ave	123	4604	
	4 Jones	iorbes ave	123	4004	
+ 12	3 smith	main str	234	5614	B
23	4 jones	forbes ave	234	5614	В
	, , , , , ,				



FUNDAMENTAL Relational operators

selection

$$\sigma_{condition}$$
 (F

projection

$$\pi_{_{att-list}}(R)$$

cartesian product

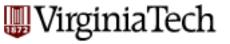
MALE x FEMALE

set union

 $R \cup S$

set difference

R-S



Relational ops

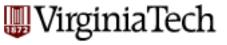
- Surprisingly, they are enough, to help us answer almost any query we want!!
- derived/convenience operators:
 - set intersection
 - join (theta join, equi-join, natural join)
 - 'rename' operator $\rho_{R'}(R)$
 - division $R \div S$



Joins

Equijoin:

$$R \bowtie_{R,a=S,b} S = \sigma_{R,a=S,b}(R \times S)$$



Cartesian product

■ A: $\sigma_{STUDENT.ssn=TAKES.ssn}(STUDENT \ x \ TAKES)$

<u>Ssn</u>	Name	Address	ssn	cid	grade
123	smith	main str	123	4604	Α
224	jones	foulce	400	4004	Α
234	Jones	ioines ave	123	4004	A
123	emith	main etr	23/	561 <i>1</i>	R
120	Ommen	mam st	201	0017	
234	jones	forbes ave	234	5614	В

₩VirginiaTech

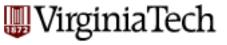
Joins

- Equijoin: $R \bowtie_{R.a=S.b} S = \sigma_{R.a=S.b}(R \times S)$
- \blacksquare theta-joins: $R \bowtie_{\theta} S$ generalization of equi-join any condition θ



Joins

- very popular: natural join: R ⋈S
- like equi-join, but it drops duplicate columns:
 STUDENT (ssn, name, address)
 TAKES (ssn, cid, grade)



Joins

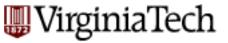
■ nat. join has 5 attributes *STUDENT* ► *TAKES*

<u>S</u>	<u>sn</u>	Name	Address	ssn	cid	grade
	123	smith	main str	123	4604	Α
	234	jones	forbes ave	123	4604	Α
	123	smith	main str	234	5614	В
	234	jones	forbes ave	234	5614	В

equi-join: 6

STUDENT STUDENT .ssn=TAKES .ssn

TAKES



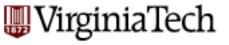
Natural Joins - nit-picking

if no attributes in common between R, S:
 nat. join -> cartesian product

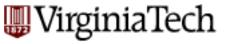


Overview - rel. algebra

- fundamental operators
- derived operators
 - joins etc
 - rename
 - division
- examples



- Q: why? $\rho_{AFTER}(BEFORE)$
- A: shorthand; self-joins; ...
- for example, find the grand-parents of 'Tom', given PC (parent-id, child-id)



■ PC (parent-id, child-id) $PC \bowtie PC$

PC		PC	
p-id	c-id	p-id	c-id
Mary	Tom	Mary	Tom
Peter	Mary	Peter	Mary
John	Tom	John	Tom



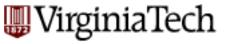
first, WRONG attempt:





- (why? how many columns?)
- Second WRONG attempt:

$$PC \bowtie_{PC.c-id=PC.p-id} PC$$



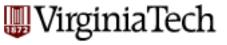
we clearly need two different names for the same table - hence, the 'rename' op.

$$\rho_{PC1}(PC)$$
 \triangleright \downarrow $PC1.c-id=PC.p-id$ PC

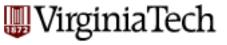


Overview - rel. algebra

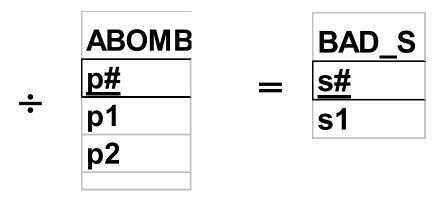
- fundamental operators
- derived operators
 - joins etc
 - rename
 - division
- examples



- Rarely used, but powerful.
- Example: find suspicious suppliers, ie., suppliers that supplied all the parts in A_BOMB



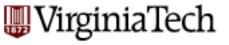
SHIPMENT	
<u>s#</u>	<u>p#</u>
s 1	p1
s2	p1
s1	p2
s3	p1
s 5	p3



Example: find suspicious suppliers, ie., suppliers that supplied all the parts in A_BOMB



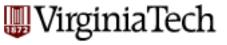
- Observations: ~reverse of cartesian product
- It can be derived from the 5 fundamental operators (!!)
- How?



Answer:

$$r \div s = \pi_{(R-S)}(r) - \pi_{(R-S)}[(\pi_{(R-S)}(r) \times s) - r]$$

 Observation: find 'good' suppliers, and subtract! (double negation)

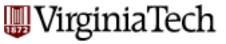


Answer:

SHIPMENT	
<u>s#</u> s1	<u>p#</u>
s1	p1
s2	p1
s1	p2
s3	p1
s 5	р3

$$r \div s = \pi_{(R-S)}(r) - \pi_{(R-S)}[(\pi_{(R-S)}(r) \times s) - r]$$

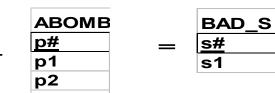
 Observation: find 'good' suppliers, and subtract! (double negation)



Answer:

Table 'r'

SHIPMENT	
<u>s#</u>	<u>p#</u>
<u>s#</u> s1	p1
s2	p1
s1	p2
s3	p1
s5	р3



$$r \div S = \pi_{(R-S)}(r) - \pi_{(R-S)}[(\pi_{(R-S)}(r) \times S) - r]$$

All suppliers

All bad parts



Answer:

Table 'r' SHIPMENT s# p# s1 p1 s2 p1 s1 p2 s3 p1

р3

Table 's'

ABOMB
BAD_S

$$r \div s = \pi_{(R-S)}(r) - \pi_{(R-S)}[(\pi_{(R-S)}(r) \times s) - r]$$

s5



all possible suspicious shipments



Answer:

Table 'r' **SHIPMENT** p# s# **s**1 р1 **s2** р1

p2

р1

р3

ABOMB <u>p#</u> р1 **p2**

$$r \div s = \pi_{(R-S)}(r) - \pi_{(R-S)}[(\pi_{(R-S)}(r) \times s) - r]$$

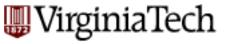
s1

s3

s5



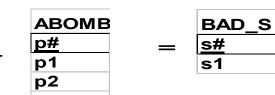
all possible suspicious shipments that didn't happen



Answer:

Table 'r'

SHIPMENT	
<u>s#</u>	<u>p#</u>
s1	p1
s2	p1
s1	p2
s3	p1
s 5	р3



$$r \div s = \pi_{(R-S)}(r) - \pi_{(R-S)}[(\pi_{(R-S)}(r) \times s) - r]$$

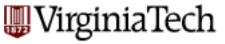


all suppliers who missed at least one suspicious shipment, i.e.: 'good' suppliers



Overview - rel. algebra

- fundamental operators
- derived operators
 - joins etc
 - rename
 - division
- examples



Sample schema

find names of students that take 4604

STUDENT		
<u>Ssn</u>	Name	Address
123	smith	main str
234	jones	forbes ave

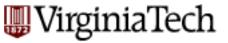
CLA55			
<u>c-id</u>	c-name	units	
4513	s.e.		2
4512	o.s.		2

TAKES

<u>SSN</u>	<u>c-id</u>	grade
123	4513	Α
234	4513	В

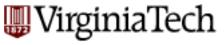


find names of students that take 4604



find names of students that take 4604

$$\pi_{name}[\sigma_{c-id=4604}(STUDENT)]$$



Sample schema

find course names of 'smith'

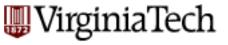
STUDENT		
<u>Ssn</u>	Name	Address
123	smith	main str
234	jones	forbes ave

CLA33			
c-id	c-name	units	
4613	s.e.	2	
4612	o.s.	2	

CLACC

TAKES

<u>SSN</u>	<u>c-id</u>	grade
123	4613	Α
234	4613	В



find course names of 'smith'

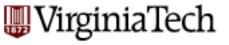
$$\pi_{c-name}[\sigma_{name='smith'}]$$

STUDENT \ TAKES \ CLASS

)]



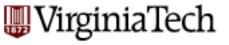
find ssn of 'overworked' students, ie., that take 4612, 4613, 4604



find ssn of 'overworked' students, ie., that take 4612, 4613, 4604: almost correct answer:

$$\sigma_{c-name=4612}(TAKES) \cap$$
 $\sigma_{c-name=4613}(TAKES) \cap$
 $\sigma_{c-name=4604}(TAKES)$



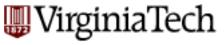


find ssn of 'overworked' students, ie., that take 4612, 4613, 4604 - Correct answer:

$$\pi_{ssn}[\sigma_{c-name=4612}(TAKES)] \cap \\ \pi_{ssn}[\sigma_{c-name=4613}(TAKES)] \cap \\ \pi_{ssn}[\sigma_{c-name=4604}(TAKES)]$$



find ssn of students that work at least as hard as ssn=123, ie., they take all the courses of ssn=123, and maybe more



Sample schema

STUDENT		
<u>Ssn</u>	Name	Address
123	smith	main str
234	jones	forbes ave

CLASS			
<u>c-id</u>	c-name	units	
4613	s.e.		2
4612	o.s.		2

CIACC

TAKES

<u>SSN</u>	<u>c-id</u>	grade
123	4613	Α
234	4613	В



find ssn of students that work at least as hard as ssn=123 (ie., they take all the courses of ssn=123, and maybe more

$$[\pi_{ssn,c-id}(TAKES)] \div \pi_{c-id}[\sigma_{ssn=123}(TAKES)]$$



Conclusions

- Relational model: only tables ('relations')
- relational algebra: powerful, minimal: 5 operators can handle almost any query!