

SQL and Relational Algebra

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What is SQL?

- ▶ SQL = Structured Query Language (pronounced “sequel”).
- ▶ Language for defining *as well as* querying data in an RDBMS.
- ▶ Primary mechanism for querying and modifying the data in an RDBMS.
- ▶ SQL is declarative:
 - ▶ Say what you want to accomplish, without specifying how.
 - ▶ One of the main reasons for the commercial success of RDBMSs.
- ▶ SQL has many standards and implementations:
 - ▶ ANSI SQL
 - ▶ SQL-92/SQL2 (null operations, outerjoins)
 - ▶ SQL-99/SQL3 (recursion, triggers, objects)
 - ▶ Vendor-specific variations.

What is Relational Algebra?

- ▶ Relational algebra is a notation for specifying queries about the contents of relations.
- ▶ Relational algebra eases the task of reasoning about queries.
- ▶ Operations in relational algebra have counterparts in SQL.
- ▶ To process a query, a DBMS translates SQL into a notation similar to relational algebra.

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 - ▶ Set algebra: operands are sets and operators are \cup , \cap , $-$.
- ▶ An algebra allows us to construct expressions by combining operands and expression using operators and has rules for reasoning about expressions.
 - ▶ $a^2 + 2 \times a \times b + b^2, (a + b)^2$.
 - ▶ $R - (R - S), R \cap S$.

Basics of Relational Algebra

- ▶ Operands are relations, thought of as sets of tuples.
- ▶ Think of operands as variables, whose tuples are unknown.
- ▶ Results of operations are also sets of tuples. (Later, we will define a relational algebra on bags.)
- ▶ Think of expressions in relational algebra as *queries*, which construct new relations from given relations.
- ▶ Four types of operators:
 - ▶ Remove parts of a single relation: projection and selection.
 - ▶ Usual set operations (union, intersection, difference).
 - ▶ Combine the tuples of two relations, such as cartesian product and joins.
 - ▶ Renaming.

Projection

- ▶ The *projection* operator produces from a relation R a new relation containing only some of R 's columns.
- ▶ To obtain a relation containing only the columns A_1, A_2, \dots, A_n of R

RA $\pi_{A_1, A_2, \dots, A_n}(R)$
SQL SELECT A_1, A_2, \dots, A_n
FROM R;

Selection

- ▶ The *selection* operator applied to a relation R produces a new relation with a subset of R 's tuples.
- ▶ The tuples in the resulting relation satisfy some condition C that involves the attributes of R .

RA $\sigma_C(R)$
SQL SELECT *
FROM R
WHERE C;

- ▶ The WHERE clause of an SQL command corresponds to $\sigma()$.

Selection: Syntax of Conditional

- ▶ Syntax of *C*: similar to conditionals in programming languages. Values compared are constants and attributes of the relations mentioned in the *FROM* clause.
- ▶ We may apply usual arithmetic operators to numeric values before comparing them.
 - RA Compare values using standard arithmetic operators.
 - SQL Compare values using =, <>, <, >, <=, >=.

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RA $R \cup S$
SQL (SELECT * FROM R)
UNION
(SELECT * FROM S);

Set Operations: Intersection

- ▶ The *intersection* of two relations R and S is the set of tuples that are in both R and S .
- ▶ Same conditions hold on R and S as for the union operator.

RA $R \cap S$
SQL (SELECT * FROM R)
INTERSECT
(SELECT * FROM S);

Set Operations: Difference

- ▶ The *difference* of two relations R and S is the set of tuples that are in R but not in S .
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- ▶ $R - (R - S) = R \cap S$.
- ▶ Compare to

(SELECT * FROM R)
EXCEPT
((SELECT * FROM R)
EXCEPT
(SELECT * FROM S));

(SELECT * FROM R);
INTERSECT
(SELECT * FROM S);

Cartesian Product

- ▶ The *Cartesian product* (or *cross-product* or *product*) of two relations R and S is a the set of pairs that can be formed by pairing each tuple of R with each tuple of S .
 - ▶ The result is a relation whose schema is the schema for R followed by the schema for S .
 - ▶ We rename attributes to avoid ambiguity or we prefix attribute with the name of the relation it belongs to.

RA $R \times S$
SQL SELECT *
FROM R, S;

Theta-Join

- ▶ The *theta-join* of two relations R and S is the set of tuples in the Cartesian product of R and S that satisfy some condition C .

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- ▶ $R \bowtie_C S = \sigma_C(R \times S)$.

Natural Join

- ▶ The *natural join* of two relations R and S is a set of pairs of tuples, one from R and one from S , that agree on whatever attributes are common to the schemas of R and S .
- ▶ The schema for the result contains the union of the attributes of R and S .
- ▶ Assume the schemas $R(A, B, C)$ and $S(B, C, D)$.

RA $R \bowtie S$

```
SQL SELECT R.A, R.B, R.C, S.D
      FROM R,S
      WHERE R.B = S.B AND R.C = S.C;
```

- ▶ A *dangling tuple* is one that fails to pair with any tuple in the other relation.

Operators Covered So Far

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- ▶ Set operations (R and S must have the same attributes, same attribute types, and same order of attributes):
 - ▶ union: $R \cup S$ and (R) UNION (S).
 - ▶ intersection: $R \cap S$ and (R) INTERSECT (S).
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- ▶ Combine the tuples of two relations:
 - ▶ Cartesian product: $R \times S$ and `... FROM R, S ...`
 - ▶ Theta-join: $R \underset{C}{\bowtie} S$ and `... FROM R, S WHERE C.`
 - ▶ Natural join: $R \bowtie S$; in SQL, list the conditions that the common attributes be equal in the WHERE clause.

Other Details in SQL

- ▶ Read Chapters 6.1.3-6.1.8 of the textbook for strings comparison, pattern matching, NULL and UNKNOWN values, dates and times, and ordering the output.

Independence of Operators

- ▶ The operators we have covered so far are: $\pi_{A,B}(R)$, $\sigma_C(R)$, $\rho_{S(A_1,A_2)}(R)$, $R \cup S$, $R \cap S$, $R - S$, $R \times S$, $R \bowtie S$, $R \bowtie_C S$.
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 $R.A_1 = S.A_1$ AND $R.A_2 = S.A_2$ AND ... AND $R.A_n = S.A_n$
 - ▶ $R \bowtie S = \pi_L(\sigma_C(R \times S))$
- ▶ All other operators are independent, i.e., no operator can be written in terms of the others.

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- ▶ How do we answer the query “Name pairs of students who live at the same address”?
 - ▶ We need to take the cross-product of `Students` with itself.
 - ▶ How do we refer to the two “copies” of `Students`?
 - ▶ Use the rename operator.

RA $\rho_S(A_1, A_2, \dots, A_n)(R)$: give R the name S ; R has n attributes, which are called A_1, A_2, \dots, A_n in S .

SQL Use the `AS` keyword in the `FROM` clause: `Students AS Students1` renames `Students` to `Students1`.

SQL Use the `AS` keyword in the `SELECT` clause to rename attributes.

Example of Renaming

- ▶ Name pairs of students who live at the same address.

RA $\pi_{S1.Name, S2.Name}(\sigma_{S1.Address = S2.Address}(\rho_{S1}(Students) \times \rho_{S2}(Students)))$.

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FROM Students AS S1, Students AS S2
WHERE S1.address = S2.address;`

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- ▶ Add the condition `S1.name < S2.name`.

Example RA/SQL Queries

Solve problems in Handout 1.