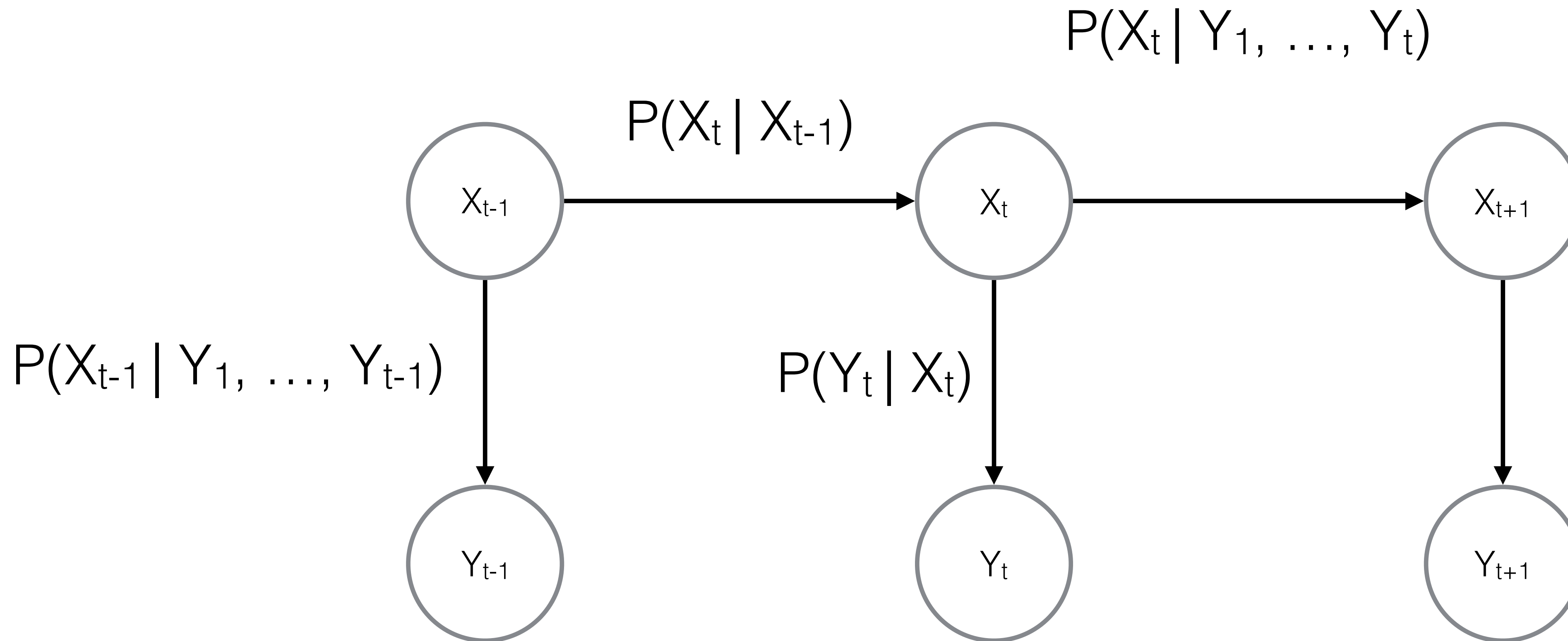


Particle Filters

Particle Filters

- Sample-based approximation of full inference
- Plan
 - Review full inference for tracking
 - Particle filter approximation

Inference for Live Tracking



Inference for Live Tracking

$$P(X_t | Y_1, \dots, Y_t)$$

$$P(Y_t | X_t) P(X_t | X_{t-1}) P(X_{t-1} | Y_1, \dots, Y_{t-1})$$

$$P(Y_t | X_t) P(X_t, X_{t-1} | Y_1, \dots, Y_{t-1})$$

$$P(Y_t, X_t, X_{t-1} | Y_1, \dots, Y_{t-1})$$

$$P(Y_t = y, X_t | Y_1, \dots, Y_{t-1}) = \sum_x P(Y_t = y, X_t = x | Y_1, \dots, Y_{t-1})$$

$$P(Y_t = y | Y_1, \dots, Y_{t-1}) = \sum_x P(Y_t = y, X_t = x | Y_1, \dots, Y_{t-1})$$

$$P(X_t | Y_1, \dots, Y_t) = \frac{P(Y_t = y, X_t | Y_1, \dots, Y_{t-1})}{\sum_x P(Y_t = y, X_t = x | Y_1, \dots, Y_{t-1})}$$

Inference for Live Tracking

$$P(X_t | Y_1, \dots, Y_t) = \frac{P(Y_t = y, X_t | Y_1, \dots, Y_{t-1})}{\sum_x P(Y_t = y, X_t | Y_1, \dots, Y_{t-1})}$$

transition
probability

$$P(X_t | Y_1, \dots, Y_t) \propto \sum_x P(Y_t | X_t) P(X_t | X_{t-1}=x) P(X_{t-1}=x | Y_1, \dots, Y_{t-1})$$

observation
probability

computed from
previous time step

Computational Cost

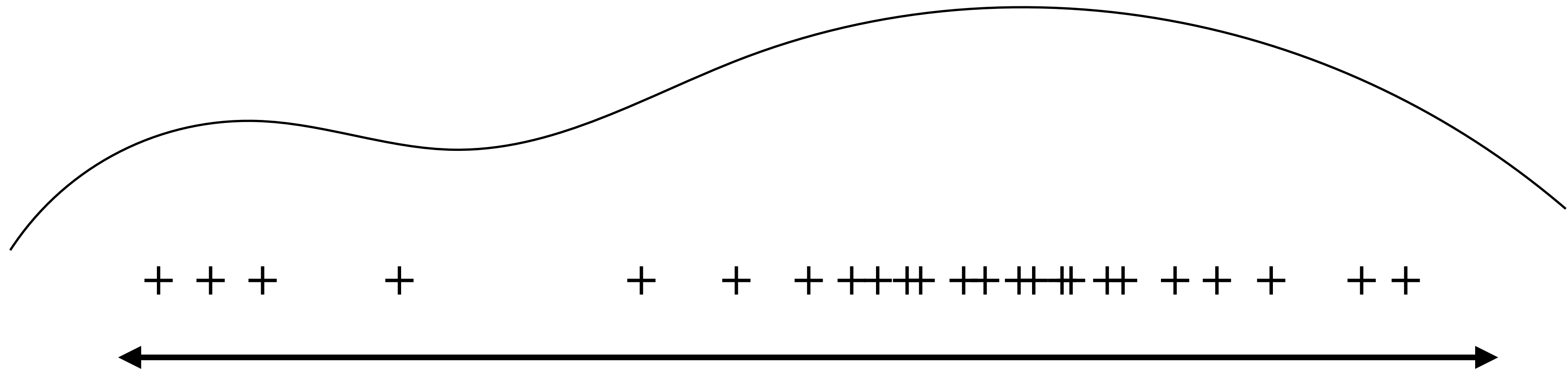
$$\sum_x P(Y_t | X_t) P(X_t | X_{t-1}=x) P(X_{t-1}=x | Y_1, \dots, Y_{t-1})$$

For all X_t states, sum over all possible X_{t-1} states

$$\text{cost: } |X_t| |X_{t-1}|$$

$|X|$ is how many states in the environment. Could be huge!

Particle Filtering



Step 1: Transition

$$P(X_t | X_{t-1})$$

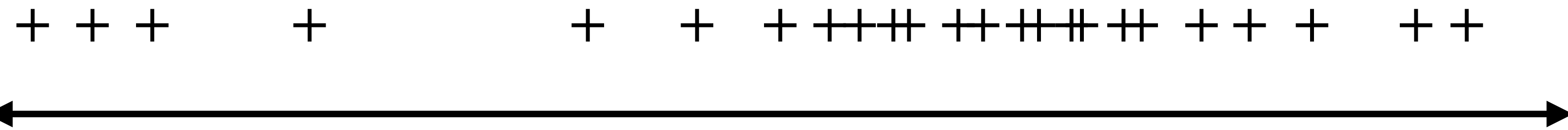
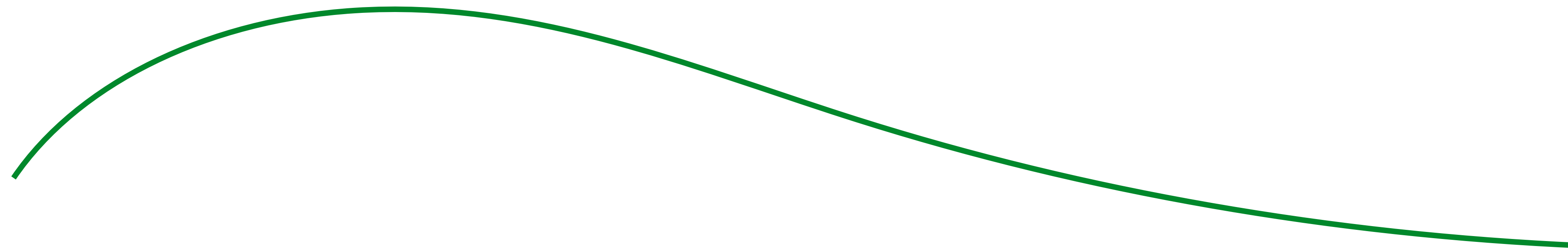
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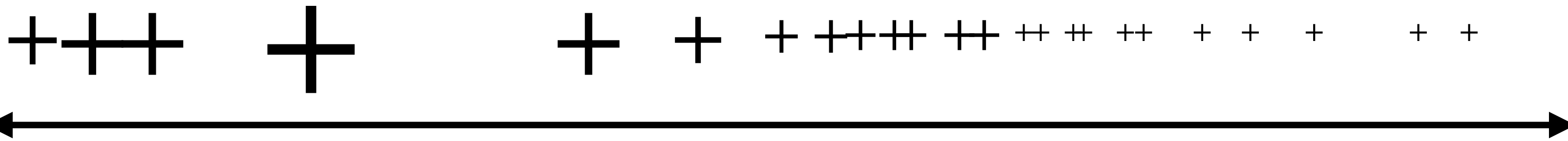
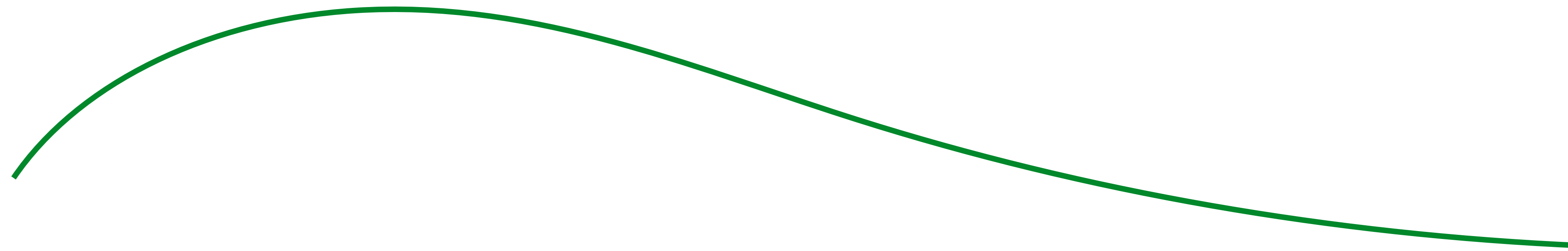
Step 2: Reweighting

$P(Y_t | X_t)$



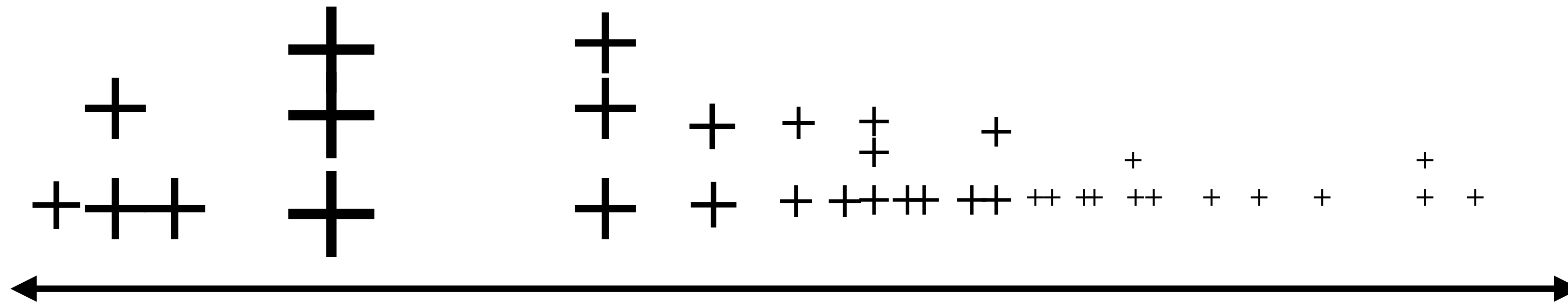
Step 2: Reweighting

$P(Y_t | X_t)$



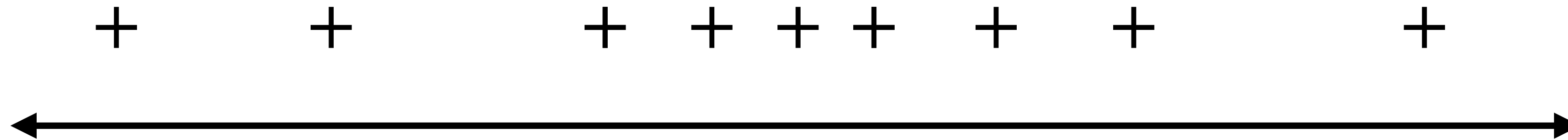
Step 3: Resampling

$P(Y_t | X_t)$



Step 3: Resampling

$P(Y_t | X_t)$



Particle Filtering

- Use n “particles” to represent distribution over hidden states
 - Transition: sample next state for each particle
 - Evidence: weight samples based on evidence
 - Resample to generate a new distribution of particles