Logic Programming, Prolog

In Text: Chapter 16

Overview

- Logic programming
- Formal logic
- Prolog

Logic Programming

- To express programs in a form of symbolic logic, and use a logic inferencing process to produce results
 - Symbolic logic is the study of symbolic abstractions that capture the formal features of logical inference
- Logic programs are declarative

Formal Logic

- A proposition is a logical statement or query about the state of the "universe"
 - It consists of objects and the relationship between objects
- Formal logic was developed to describe propositions, with the goal of allowing those formally stated propositions to be checked for validity

Symbolic Logic

- Symbolic logic can be used for three basic needs of formal logic
 - To express propositions,
 - To express the relationship between propositions, and
 - To describe how new propositions can be inferred from other propositions that are assumed to be true

Formal logic & mathematics

- Most of mathematics can be thought of in terms of logic
- The fundamental axioms of number and set theory are the initial set of propositions, which are assumed to be true
- Theorems are the additional propositions that can be inferred from the initial set

First-Order Predicate Calculus

- The particular form of symbolic logic that is used for logic programming is called first-order predicate calculus
- It contains propositions and clausal form

Propositions

- The objects in propositions are represented by simple terms
 - Simple terms can be either constants or variables
 - A constant is a symbol that represents an object
 - A variable is a symbol that can represent different objects at different times

Propositions (cont'd)

- The simplest propositions, which are called atomic propositions, consist of compound terms
- A compound term represents mathematical relation. It contains
 - a functor: the function symbol that names the relation, and
 - an ordered list of parameters

Compound Terms

- A compound term with a single parameter is a 1-tuple
 - E.g. man(jake)
- A compound term with two parameters is a 2-tuple
 - E.g., like(bob, steak)

Compound Terms

- All of the simple terms in the propositions, such as man, jake, like, bob, and steak, are constants
- They mean whatever we want them to mean
 - E.g., like(bob, steak) may mean
 - · Bob likes steak, or
 - steak likes Bob, or
 - Bob is in some way similar to a steak, or
 - Does Bob like steak?
- Propositions can also contain variables, such as man(X)

Compound Propositions

 Atomic proposition(s) are connected by logical connectors

<u>Name</u>	<u>Symbol</u>	<u>Example</u>	<u>Meaning</u>
negation	¬	¬a	not a
conjunction	\cap	$a \cap b$	a and b
disjunction	U	$a \cup b$	a or b
equivalence	≡	$a \equiv b$	a is equivalent to b
implication	\supset	$a \supset b$	a implies b b implies a
		$a \subset b$	b implies a

Compound Propositions (cont'd)

- Quantifiers—used to bind variables in propositions
 - Universal quantifier: ∀
 ∀X.P means "for all X, P is true"
 - Existential quantifier: 3
 - $\exists X.P$ means "there exists a value of X such that P is true"
 - Examples
 - $\forall X.(manager(X) \supset employee(X))$
 - $\exists X.(mother(mary,X) \cap male(X))$

Clausal Form

- Clausal form is a standard form of propositions
- It can be used to simplify computation by an automated system

Clausal Form

 A proposition in clausal form has the following general syntax:

 $\underline{\mathsf{B1} \cup \mathsf{B2} \cup ... \cup \mathsf{Bn}} \subset \mathsf{A1} \cap \mathsf{A2} \cap ... \cap \mathsf{Am}$

consequent

antecedent

- Consequent is the consequence of the truth of the antecedent
- Meaning
 - If all of the A's are true, then at least one
 B is true

Examples

- likes(bob, mcintosh) ⊂ likes(bob, apple)
 ∩ apple(mcintosh)
- father(john, alvin) ∪ father(john, alice)

 □ father(alvin, bob) ∩ mother(alice, bob) ∩ grandfather(john, bob)

Predicate Calculus

- Predicate calculus describes collections of propositions
- Resolution is the process of inferring propositions from given propositions
- Resolution can detect any inconsistency in a given set of proposition

An Exemplar Resolution

- If we know: older(terry, jon) ⊂ mother(terry, jon) wiser(terry, jon) ⊂ older(terry, jon)

Horn Clauses

- When propositions are used for resolution, only Horn clauses can be used
- A proposition with zero or one term in the consequent is called a Horn clause
 - If there is only one term in the consequence, the clause is called a Headed Horn clause

 - For stating Inference Rules in Prolog
 - If there is no term in the consequence, the clause is called a Headless Horn clause
 - E.g., man(jake)
 - · For stating Facts and Queries in Prolog

Logic Programming Languages

- Logical programming languages are declarative languages
- Declarative semantics: It is simple to determine the meaning of each statement, and it does not depend on how the statement might be used to solve a problem
 - E.g., the meaning of a proposition can be concisely determined from the statement itself

Logic Programming Languages (cont'd)

- Logical Programming Languages are nonprocedural
- Instead of specifying how a result is computed, we describe the desired result and let the computer figure out how to compute it

An Example

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 E.g., sort a list
     sort(new_list, old_list) ⊂ permute(old_list,
     new_list) ∩ sorted(new_list)
     sorted(list) ⊂ ∀j such that 1 ≤ j < n,
     list(j-1) ≤ list(j)</li>
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where permute is a predicate that returns true if its second parameter is a permutation of the first one

Key Points about Logic Programming

- Nonprocedural programming sounds like the mere production of concise software requirements specifications
 - It is a fair assessment
- Unfortunately, logic programs that use only resolution face the problems of execution efficiency

- The best form of a logic language has not been determined
- Good methods of creating programs in logic programming languages have not yet been developed