

Attribute Evaluation Order

- Determining attribute evaluation order for any attribute grammar is a complex problem, requiring the construction of a dependency graph to show all attribute dependencies

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Decoration of a parse tree for the val attribute evaluation of $(1 + 3) * 2$

$E_1 \rightarrow E_2 + T$	$E1.val = E2.val + T.val$
$E_2 \rightarrow E_2 - T$	$E1.val = E2.val - T.val$
$E \rightarrow T$	$E.val = T.val$
$T_1 \rightarrow T_2 * F$	$T1.val = T2.val * F.val$
$T_1 \rightarrow T_2 / F$	$T1.val = T2.val / F.val$
$T \rightarrow F$	$T.val = F.val$
$F_1 \rightarrow - F_2$	$F1.val = - F2.val$
$F \rightarrow (E)$	$F.val = E.val$
$F \rightarrow const$	$F.val = C.val$

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Attribute Grammar for Constant Expressions based on LL(1) CFG

- $E \rightarrow T TT$
 $\triangleright TT.st := T.val \quad \triangleright E.val := TT.val$
- $TT_1 \rightarrow + T TT_2$
 $\triangleright TT_2.st := TT_1.st + T.val \quad \triangleright TT_1.val := TT_2.val$
- $TT_1 \rightarrow - T TT_2$
 $\triangleright TT_2.st := TT_1.st - T.val \quad \triangleright TT_1.val := TT_2.val$
- $TT \rightarrow \epsilon$
 $\triangleright TT.val := TT.st$
- $T \rightarrow F FT$
 $\triangleright FT.st := F.val \quad \triangleright T.val := FT.val$
- $FT_1 \rightarrow * F FT_2$
 $\triangleright FT_2.st := FT_1.st \times F.val \quad \triangleright FT_1.val := FT_2.val$
- $FT_1 \rightarrow / F FT_2$
 $\triangleright FT_2.st := FT_1.st \div F.val \quad \triangleright FT_1.val := FT_2.val$
- $FT \rightarrow \epsilon$
 $\triangleright FT.val := FT.st$
- $F_1 \rightarrow - F_2$
 $\triangleright F_1.val := - F_2.val$
- $F \rightarrow (E)$
 $\triangleright F.val := E.val$
- $F \rightarrow const$
 $\triangleright F.val := const.val$

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Attribute Grammar for CE LL(1) CFG

- Attributes
 - *st*: subtotal attribute to record intermediate evaluation result so far
 - *val*: value attribute to copy the right-most leaf back up to the root

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Decoration of parse tree for $(1 + 3) * 2$

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Program Assignment 2 Due date: 11/9 12:30pm

- Bitwise Manipulation of Hexadecimal Numbers
- CFG

$E \rightarrow E \text{ " " } A$	bitwise OR
$E \rightarrow A$	
$A \rightarrow A \text{ "^" } B$	bitwise XOR
$A \rightarrow B$	
$B \rightarrow B \text{ "&" } C$	bitwise AND
$B \rightarrow C$	
$C \rightarrow \text{ "<" } C$	bitwise shift left 1
$C \rightarrow \text{ ">" } C$	bitwise shift right 1
$C \rightarrow \text{ "~" } C$	bitwise NOT
$C \rightarrow \text{ "(" } E \text{ ")"}$	
$C \rightarrow \text{ hex}$	

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LL(1) Attribute Grammar

```

E -> A EE
EE.st = A.val    E.val = EE.val

EE -> | A EE;
EE.st = EE.st | A.val    ( "|" bitwise OR )
EE.val = EE.val

EE -> ε
EE.val = EE.st

A -> B AA
AA.st = B.val    A.val = AA.val

AA -> ε | B AA;
AA.st = AA.st | B.val    ( "|" bitwise XOR )
AA.val = AA.val

AA -> ε
AA.val = AA.st

B -> C BB
BB.st = C.val    B.val = BB.val

BB -> ε | C BB;
BB.st = BB.st | C.val    ( "&" bitwise AND )
BB.val = BB.val

BB -> ε
BB.val = BB.st

Ci -> <C>
Ci.val = Ci.val << 1    ( "<<" bitwise shift left one )

Ci -> >C>
Ci.val = Ci.val >> 1    ( ">>" bitwise shift right one )

Ci -> ~C>
Ci.val = ~Ci.val    ( "~" bitwise NOT )

C -> ( E )
C.val = E.val

C -> hex
C.val = hex.val
    
```

Program Requirement

- Write a C program using recursive descent parser w/ lexical analyzer to implement the designated inherited and synthesized attributes. The program evaluates the expressions in a file input.txt, and outputs the results to console
- E.g., input: f&a
output: f&a = a

Program Requirements

- You cannot use more than 2 global/non-local variables, and they should be to hold the Operator and HexNumber as detected by the lexical analyzer

Hints

- To solve the problems, you should take the following steps:
 - Write a lexical analyzer
 - Write a recursive-descent parser
 - Attributes are processed as either pass-in parameters or return value of functions

Hints

- Write a lexical analyzer
 - You may need to define an enum type for all possible tokens your scanner can generate
 - E.g., when reading hexadecimal numbers 0-9 or a-f, the recognized token is HEX, and the value is saved in HexNumber

Hints

- Write a recursive-descent parser
 - Parse the program by defining and invoking functions
 - E.g.,


```

E -> A EE
EE.st = A.val
E.val = EE.val

int E() {
    int val = A();
    return EE(val);
}
                    
```

Hints

- There are parameters passed in or returned when invoking functions. When invoking a function, the synthesized attribute is the return value, while the inherited attribute is the passing-in parameter

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Hints

- Sample code of main()

```
int main() {
    int val;
    symbol = getNextToken();
    while (symbol != EOF_) {
        if (symbol != NEW_LINE) {
            val = E();
            printf(" = %x\n", val & 0xf);
        }
        if (symbol == EOF_) break;
        symbol = getNextToken();
    }
    return 1;
}
```

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Submission Requirements

- Pack the following files into a .tar file:
 - Source file: parser.c
 - Executable file: parser
 - Input file: input.txt
 - Output file: output.txt (copy all your console outputs to this file)
 - README file (optional, used if you have any additional comments/explanations about the files)

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DYNAMIC SEMANTICS

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Dynamic Semantics

- Describe the meaning of expressions, statements, and program units
- No single widely acceptable notation or formalism for describing semantics
- Two common approaches:
 - Operational
 - Denotational

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Operational Semantics

- Gives a program's meaning in terms of its implementation on a **real or virtual machine**
- **Change in the state** of the machine (memory, registers, etc.) defines the meaning of the statement

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Operational Semantics Definition Process

1. Design an appropriate intermediate language. Each construct of the intermediate language must have an obvious and unambiguous meaning
2. Construct a virtual machine (an interpreter) for the intermediate language. The virtual machine can be used to execute either single statements, code segments, or whole programs

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An Example

C	Operational Semantics
<pre>for (expr1; expr2; expr3) { . . . }</pre>	<pre>expr1; loop: if expr2 == 0 goto out . . . expr3; goto loop out: . . .</pre>

- The virtual computer is supposed to be able to correctly "execute" the instructions and recognize the effects of the "execution"

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Key Points of Operational Semantics

- Advantages
 - May be simple and intuitive for small examples
 - Good if used informally
 - Useful for implementation
- Disadvantages
 - Very complex for large programs
 - Lacks mathematical rigor

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Typical Usage of Operational Semantics

- Vienna Definition Language (VDL) used to define PL/I (Wegner 1972)
- Unfortunately, VDL is so complex that it serves no practical purpose

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Denotational Semantics

- The most rigorous, widely known method for describing the meaning of programs
- Solely based on recursive function theory
- Originally developed by Scott and Strachey (1970)

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Denotational Semantics

- Key Idea
 - Define for each language entity both a mathematical object, and a function that maps instances of that entity onto instances of the mathematical object
- The basic idea
 - There are rigorous ways of manipulating mathematical objects but not programming language constructs

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Denotational Semantics

- Difficulty
 - How to create the objects and the mapping functions?
- The method is named *denotational*, because the mathematical objects denote the meaning of their corresponding syntactic entities

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Denotational vs. Operational

- Both denotational semantics and operational semantics are defined in terms of state changes in a virtual machine
- In operational semantics, the state changes are defined by **coded algorithms** in the machine
- In denotational semantics, the state change is defined by **rigorous mathematical functions**

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Program State

- Let the state *s* of a program be a set of pairs as follows:
 - $\{ \langle i_1, v_1 \rangle, \langle i_2, v_2 \rangle, \dots, \langle i_n, v_n \rangle \}$
 - Each *i* is the name of a variable
 - The associated *v* is the current value of the variable
 - Any *v* can have the special value **undef**, indicating that the associated variable is undefined
- Let VARMAP be a function as follows:

$$\text{VARMAP}(i_j, s) = v_j$$

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Program State

- Most semantics mapping functions for programs and program constructs map from states to states
- These state changes are used to define the meanings of programs and program constructs
- Some language constructs, such as expressions, are mapped to values, not state changes

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An Example

- CFG for binary numbers
 - $\langle \text{bin_num} \rangle \rightarrow '0'$
 - $\langle \text{bin_num} \rangle \rightarrow '1'$
 - $\langle \text{bin_num} \rangle \rightarrow \langle \text{bin_num} \rangle '0'$
 - $\langle \text{bin_num} \rangle \rightarrow \langle \text{bin_num} \rangle '1'$
- Parse tree of the binary number 110


```

                    <bin_num>
                   /  \
                <bin_num> '0'
               /  \
            <bin_num> '1'
           /  \
          '1'  <bin_num>
                /  \
               '1' '0'
            
```

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Example Semantic Rule Design

- Mathematical objects
 - Decimal number equivalence for each binary number
- Functions
 - Map binary numbers to decimal numbers
 - Rules with terminals as RHS are translated as direct mappings from terminals to mathematical objects
 - Rules with nonterminals as RHS are translated as manipulations on mathematical objects

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Example Semantic Rules

Syntax Rules	Semantic Rules
$\langle \text{bin_num} \rangle \rightarrow '0'$	$M_{\text{bin}}('0') = 0$
$\langle \text{bin_num} \rangle \rightarrow '1'$	$M_{\text{bin}}('1') = 1$
$\langle \text{bin_num} \rangle \rightarrow \langle \text{bin_num} \rangle '0'$	$M_{\text{bin}}(\langle \text{bin_num} \rangle '0') =$ $2 * M_{\text{bin}}(\langle \text{bin_num} \rangle)$
$\langle \text{bin_num} \rangle \rightarrow \langle \text{bin_num} \rangle '1'$	$M_{\text{bin}}(\langle \text{bin_num} \rangle '1') =$ $2 * M_{\text{bin}}(\langle \text{bin_num} \rangle) + 1$

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Expressions

- CFG for expressions
 - $\langle \text{expr} \rangle \rightarrow \langle \text{dec_num} \rangle \mid \langle \text{var} \rangle \mid \langle \text{binary_expr} \rangle$
 - $\langle \text{binary_expr} \rangle \rightarrow \langle \text{l_expr} \rangle \langle \text{op} \rangle \langle \text{r_expr} \rangle$
 - $\langle \text{l_expr} \rangle \rightarrow \langle \text{dec_num} \rangle \mid \langle \text{var} \rangle$
 - $\langle \text{r_expr} \rangle \rightarrow \langle \text{dec_num} \rangle \mid \langle \text{var} \rangle$
 - $\langle \text{op} \rangle \rightarrow + \mid *$

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Expressions

$M_e(\langle \text{expr} \rangle, s) \Delta =$
 case $\langle \text{expr} \rangle$ of
 $\langle \text{dec_num} \rangle \Rightarrow M_{\text{dec}}(\langle \text{dec_num} \rangle)$
 $\langle \text{var} \rangle \Rightarrow \text{VARMAP}(\langle \text{var} \rangle, s)$
 $\langle \text{binary_expr} \rangle \Rightarrow$
 if $\langle \text{binary_expr} \rangle.\langle \text{op} \rangle = '+'$ then
 $M_e(\langle \text{binary_expr} \rangle.\langle \text{l_expr} \rangle, s) +$
 $M_e(\langle \text{binary_expr} \rangle.\langle \text{r_expr} \rangle, s)$
 else
 $M_e(\langle \text{binary_expr} \rangle.\langle \text{l_expr} \rangle, s) \times$
 $M_e(\langle \text{binary_expr} \rangle.\langle \text{r_expr} \rangle, s)$

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Statement Basics

- The meaning of a single statement executed in a state s is a new state s' , which reflects the effects of the statement
 $M_{\text{stmt}}(\text{stmt}, s) = s'$

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Assignment Statements

$M_a(x := E, s) \Delta =$
 $s' = \{ \langle i_1', v_1' \rangle, \langle i_2', v_2' \rangle, \dots, \langle i_n', v_n' \rangle \},$
 where for $j = 1, 2, \dots, n,$
 $v_j' = \text{VARMAP}(i_j, s)$ if $i_j \neq x$
 $v_j' = M_e(E, s)$ if $i_j = x$

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Sequence of Statements

$M_{\text{stmt}}(\text{stmt1}; \text{stmt2}, s) \Delta =$
 $M_{\text{stmt}}(\text{stmt2}, M_{\text{stmt}}(\text{stmt1}, s))$
 or
 $M_{\text{stmt}}(\text{stmt1}; \text{stmt2}, s) = s''$ where
 $s' = M_{\text{stmt}}(\text{stmt1}, s)$
 $s'' = M_{\text{stmt}}(\text{stmt2}, s')$

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Sequence of Statements

```
x := 5;
y := x + 1;
write(x * y); } P2 } P1 } P0
```

Initial state $s_0 = \langle \text{mem}_0, i_0, o_0 \rangle$
 $M_{\text{stmt}}(P_0, s_0) = M_{\text{stmt}}(P_1, \underline{M_a(x := 5, s_0)})$
 s_1

$s_1 = \langle \text{mem}_1, i_1, o_1 \rangle$ where
 $\text{VARMAP}(x, s_1) = 5$
 $\text{VARMAP}(z, s_1) = \text{VARMAP}(z, s_0)$ for all $z \neq x$
 $i_1 = i_0, o_1 = o_0$

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Sequence of Statements

```
x := 5;
y := x + 1;
write(x * y); } P2 } P1 } P0
```

$M_{\text{stmt}}(P_1, s_1) = M_{\text{stmt}}(P_2, \underline{M_a(y := x + 1, s_1)})$
 s_2

$s_2 = \langle \text{mem}_2, i_2, o_2 \rangle$ where
 $\text{VARMAP}(y, s_2) = M_e(x + 1, s_1) = 6$
 $\text{VARMAP}(z, s_2) = \text{VARMAP}(z, s_1)$ for all $z \neq y$
 $i_2 = i_1, o_2 = o_1$

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Sequence of Statements

```
x := 5;
y := x + 1;
write(x * y); } P2 } P1 } P0
```

$M_{\text{stmt}}(P_2, s_2) = M_{\text{stmt}}(\text{write}(x * y), s_2) = s_3$
 $s_3 = \langle \text{mem}_3, i_3, o_3 \rangle$ where
 $\text{VARMAP}(z, s_3) = \text{VARMAP}(z, s_2)$ for all z
 $i_3 = i_2, o_3 = o_2 \cdot M_e(x * y, s_2) = o_2 \cdot 30$

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Sequence of Statements

Therefore,
 $M_{\text{stmt}}(P, s_0) = s_3 = \langle \text{mem}_3, i_3, o_3 \rangle$ where
 $\text{VARMAP}(y, s_3) = 6$
 $\text{VARMAP}(x, s_3) = 5$
 $\text{VARMAP}(z, s_3) = \text{VARMAP}(z, s_0)$ for all $z \neq x, y$
 $i_3 = i_0$
 $o_3 = o_0 \cdot 30$

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Logical Pretest Loops

- The meaning of the loop is **the value of program variables after the loop body has been executed the prescribed number of times**, assuming there have been no errors
- The loop is converted from iteration to recursion, where the recursion control is mathematically defined by other recursive state mapping functions
- Recursion is easier to describe with mathematical rigor than iteration

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Logical Pretest Loop

- $M_l(\text{while } B \text{ do } L, s) \Delta =$
 if $M_b(B, s) = \text{false}$ then
 s
 else
 $M_l(\text{while } B \text{ do } L, M_{\text{stmt}}(L, s))$

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Posttest Loop ?

- $M_{\text{ptl}}(\text{do } L \text{ until not } B, s) \Delta = ?$

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Key Points of Denotational Semantics

- Advantages
 - **Compact & precise**, with solid mathematical foundation
 - Provide a **rigorous** way to think about programs
 - Can be used to prove the correctness of programs
 - Can be an aid to language design

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Key Points of Denotational Semantics

- Disadvantages
 - **Require mathematical sophistication**
 - Hard for programmer to use
- Uses
 - Semantics for Algol-60, Pascal, etc.
 - Compiler generation and optimization

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Summary

- Each form of semantic description has its place
- Operational semantics
 - Informally describe the meaning of language constructs in terms of their effects on an ideal machine
- Denotational semantics
 - Formally define mathematical objects and functions to represent the meanings

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