

## Bindings & Scopes

- Names can be bound to values by introducing a nested scope
- `let` takes two or more arguments:
  - The first argument is a list of pairs
    - In each pair, the first element is the name, while the second is the value/expression
  - Remaining arguments are evaluated in order
  - The value of the construct as a whole is the value of the final argument
  - E.g. `(let ((a 3)) a)`

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## let Examples

- E.g., `(let ((a 3)  
          (b 4)  
          (square (lambda (x) (* x x)))  
          (plus +))  
          (sqrt (plus (square a) (square b))))`
- The scope of the bindings produced by `let` is its second and following arguments

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## let Examples

- E.g.,  $(\text{let } ((a\ 3))$   
 $(\text{let } ((a\ 4)$   
 $(b\ a))$   
 $(+ a\ b))) \Rightarrow ?$
- b takes the value of the outer a,  
because the defined names are visible  
"all at once" at the end of the  
declaration list

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## let\* Example

- let\* makes sure that names become  
available "one at a time"
- E.g.,  $(\text{let}^*((x\ 1)\ (y\ (+ x\ 1))))$   
 $(+ x\ y) \Rightarrow ?$

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## Functions

- quote: identity function
  - When the function is given a parameter, it simply returns the parameter
  - E.g.,  $(\text{quote } A) \Rightarrow A$   
 $(\text{quote } (A B C)) \Rightarrow (A B C)$
- The common abbreviation of quote is apostrophe (`'`)
  - E.g.,  $'a \Rightarrow a$   
 $'(A B C) \Rightarrow (A B C)$

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## List Functions

- car: returns the first element of a given list
  - E.g.,  $(\text{car } '(A B C)) \Rightarrow A$   
 $(\text{car } '((A B) C D)) \Rightarrow (A B)$   
 $(\text{car } 'A) \Rightarrow ?$   
 $(\text{car } '(A)) \Rightarrow ?$   
 $(\text{car } '()) \Rightarrow ?$

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## List Functions

- `cdr`: returns the remainder of a given list after its `car` has been removed
  - E.g., `(cdr '(A B C)) => (B C)`
  - `(cdr '((A B) C D)) => (C D)`
  - `(cdr 'A) => ?`
  - `(cdr '(A)) => ?`
  - `(cdr '()) => ?`

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## List Functions

- `cons`: concatenates an element with a list
- `cons` builds a list from its two arguments
  - The first can be either an atom or a list
  - The second is usually a list
  - E.g., `(cons 'A '()) => (A)`
  - `(cons 'A '(B C)) => (A B C)`
  - `(cons '() '(A B)) => ?`
  - `(cons '(A B) '(C D)) => ?`
  - How to compose a list `(A B C)` from `A`, `B`, and `C`?

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## List Functions

- Note that cons can take two atoms as parameters, and return a dotted pair
  - E.g., (cons 'A 'B) => (A . B)
  - The dotted pair indicates that this cell contains two atoms, instead of an atom + a pointer  
or  
a pointer + a pointer

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## More Predicate Functions

- The following returns #t if the symbolic atom is of the indicated type, and #f otherwise
  - E.g., (symbol? 'a) => #t  
(symbol? '()) => #f
  - E.g., (number? '55) => #t  
(number? 55) => #t  
(number? '(a)) => #f
  - E.g., (list? '(a)) => #t
  - E.g., (null? '()) => #t

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## More Predicate Functions

- `eq?` returns true if two objects are equal through pointer comparison
  - Guaranteed to work on symbols
  - E.g., `(eq? 'A 'A) => #T`  
`(eq? 'A '(A B)) => #F`
- `equal?` recursively compares two objects to determine if they are equal
  - The objects can be symbols, atoms, numbers, and lists

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## How do we implement equal?

```
(define (atom? atm)
  (cond
    ((list? atm) (null? atm))
    (else #T)
  )
)

(define (equal? lis1 lis2)
  (cond
    ((atom? lis1) (eq? lis1 lis2))
    ((atom? lis2) #F)
    ((equal? (car lis1) (car lis2))
     (equal? (cdr lis1) (cdr lis2)))
    (else #F)
  )
)
```

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## More Examples

```
(define (member? atm lis)
  (cond
    ((null? lis) #F)
    ((eq? atm (car lis)) #T)
    (else (member? atm (cdr lis))))
  )
)

(define (append lis1 lis2)
  (cond
    ((null? lis1) lis2)
    (else (cons (car lis1)
                 (append(cdr lis1) lis2))))
  )
)
```

What is returned for the following function?

```
(member? 'b '(a (b c)))
```

Is lis2 appended to lis1, or lis1 prepended to lis2?

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## An example: apply-to-all function

```
(define (mapcar fctn lis)
  (cond
    ((null? lis) '())
    (else (cons (fctn (car lis))
                 (mapcar fctn (cdr lis)) ))
  )
)
```

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