A man who has committed a mistake and doesn't correct it is committing another mistake.

Confucius

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Inducing a Hypothesis

Inductive reasoning draws generalized conclusions from a finite collection of specific observations.

The act of inducing a conclusion should provide some degree of support for the truth of the conclusion, but cannot ensure it.

Specific observation:

Every student I have encountered at Virginia Tech is a hominid.

Generalized conclusion: All students at Virginia Tech are hominids.

The conclusion may be strengthened by an indication of how long I have been at Virginia Tech and how many students I have encountered there.

Nevertheless... the conclusion cannot be absolutely affirmed.

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Intro Problem Solving in Computer Science

Simple Induction

reason from observations of a sample group to a conclusion about a member of the larger population

17 of 20 dentists we surveyed majored in Mining Eng as undergrads.

So, there is a high probability, around 85%, that your dentist will have majored in Mining Eng as an undergrad.

This is related to *inductive generalization*, which would conclude from the same evidence that:

So, 85% of all dentists majored in Mining Eng as undergrads.

Does inductive reasoning lead to knowledge?

What justifies either of the following:

Generalizing about the properties of a class of objects based on some number of observations of particular instances of that class.

For example, the inference that "all swans we have seen are white, and therefore all swans are white," before the discovery of black swans.

Presupposing that a sequence of events in the future will occur as it always has in the past.

For example, that the laws of physics will hold as they have always been observed to hold.

The problems just considered have a hallowed history in Western philosophy, from the Greeks to David Hume and beyond...

In the end, perhaps Hume put it best:

If we be, therefore, engaged by arguments to put trust in past experience, and make it the standard of our future judgement, these arguments must be probable only, or such as regard matter of fact and real existence, according to the division above mentioned. But that there is no argument of this kind, must appear, if our explication of that species of reasoning be admitted as solid and satisfactory. We have said that all arguments concerning existence are founded on the relation of cause and effect; that our knowledge of that relation is derived entirely from experience; and that all our experimental conclusions proceed upon the supposition that the future will be conformable to the past. To endeavour, therefore, the proof of this last supposition by probable arguments, or arguments regarding existence, must be evidently going in a circle, and taking that for granted, which is the very point in question.

An Enquiry Concerning Human Understanding

So, does inductive reasoning lead to knowledge?

In some instances, perhaps... and in other instances, perhaps not.

However, there seems no alternative if we are to form any conclusions regarding real phenomena.

We may observe and induce, and maintain eternal vigilance regarding the correctness of the conclusions we induce.

Sequence Example

A common test question requiring induction is to determine the next value in an incomplete sequence of integers. For example:

11, 13, 17, 19, ??

What would the next value be?

23?

31?

Something else?

The key to induction is to look for patterns... sometimes there is no obvious pattern... and even an obvious pattern is never unique.

Final Note

Do not confuse inductive reasoning with mathematical induction.

Despite some superficial similarities, they are fundamentally different.